A Machine Learning Approach for Rainfall Estimation Integrating Heterogeneous Data Sources

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Abstract—Providing an accurate rainfall estimate at individual points is a challenging problem in order to mitigate risks derived from severe rainfall events, such as floods and landslides. Dense networks of sensors, named rain gauges (RGs), are typically used to obtain direct measurements of precipitation intensity in these points. These measurements are usually interpolated by using spatial interpolation methods for estimating the precipitation field over the entire area of interest. However, these methods are computationally expensive, and to improve the estimation of the variable of interest in unknown points, it is necessary to integrate further information. To overcome these issues, this work proposes a machine learning-based methodology that exploits a classifier based on ensemble methods for rainfall estimation and is able to integrate information from different remote sensing measurements. The proposed approach supplies an accurate estimate of the rainfall where RGs are not available, permits the integration of heterogeneous data sources exploiting both the high quantitative precision of RGs and the spatial pattern recognition ensured by radars and satellites, and is computationally less expensive than the interpolation methods. Experimental results, conducted on real data concerning an Italian region, Calabria, show a significant improvement in comparison with Kriging with external drift (KED), a well-recognized method in the field of rainfall estimation, both in terms of the probability of detection (0.58 versus 0.48) and mean-square error (0.11 versus 0.15).

Index Terms—Computational infrastructure, geophysical data, GIS, oceans and water, radar data.

I. INTRODUCTION

Accurate rainfall estimate is crucial for flood hazards protection, river basins management, erosion modeling, and other applications for hydrological impact modeling. To this aim, rain gauges (RGs) are used to obtain a direct measurement of intensity and duration of precipitations at individual sites.

In order to estimate rainfall events in areas not covered by RGs, interpolation methods computed on the basis of the values recorded by these RGs are used. Many variants of these methods have been proposed in the literature, and among them, the Kriging geostatistical method [1], [2] is one of the most used and recognized in the field.

An accurate spatial reconstruction of the rainfall field is a critical issue when dealing with heavy convective meteorological events. In particular, convective precipitations can produce highly localized heavy precipitation, not detected by sparse RGs, and floods can arise without a rainfall being detected [3]. To overcome this issue, a recent trend in the literature is to integrate heterogeneous rainfall data sources to obtain a more accurate estimate by using interpolation methods [4].

Unfortunately, the largely used ordinary Kriging (OK) can exploit only one source of data as input; therefore, Kriging with external drift (KED) was one of the most popular approaches adopted to overcome this limitation [5], [6]. Indeed, KED allows a random field to be interpolated, and different from the OK, it is able to take into account secondary information. The main problem is that these methods are computationally expensive and require a large number of resources to work properly.

A different approach relies on exploiting machine learning (ML) techniques. However, using these methods requires coping with different hard issues, i.e., unbalancing of the classes, a large number of missing attributes, and the need for working incrementally as soon as new data are available. Typically, ensemble methods are used to address these issues. Ensemble [7] is a classification technique, in which several models, first trained by using different classification algorithms or samples of data, are then combined to classify new unseen instances. In comparison with the case of using a single classification model, the ensemble paradigm permits handling the problem of unbalanced classes and reducing the variance and the bias of the error. Especially, ensemble-based techniques can be used to address the issues concerning the rainfall estimation and to support the monitoring of meteorological (intense) events. These methods are also able to capture nonlinear correlations (e.g., relations between sensor data, cloud properties, and rainfall estimate).

In order to address the main issues of rainfall estimation, in this article, an ML-based methodology, adopting a hierarchical probabilistic ensemble classifier (HPEC) for rainfall
estimation, is introduced. The proposed approach, by integrating data coming from different sources (i.e., RGs, radars, and satellites) and exploiting an undersampling technique for handling the unbalanced classes problem typical of this scenario, permits accurate estimation of the rainfall where RGs are not available.

Our approach is an effective solution for real scenarios, as in the case of an officer of the Department of Civil Protection (DCP), who has to analyze the rainfall in a specific zone presenting risks of landslides or floods. The experimental evaluation is conducted on real data concerning Calabria, a region located in the South of Italy, and provided by the DCP. Calabria is an effective test ground because of its strong climate variability and its complex orography.

Our contributions can be summarized as follows.

1) Three heterogeneous data sources (i.e., RGs, radar, and Meteosat) are integrated to generate more accurate estimates of rainfall events.
2) Different classification methods are compared on a real case concerning Calabria, a southern region in Italy, and a hierarchical probabilistic ensemble approach is proposed.
3) Different ML-based methods, pretrained only on historical data, with a widely used interpolation method in the hydrological field (i.e., KED) are compared.

The rest of this article is organized as follows. In Section II, some related works are analyzed, and the main differences with our approach are noted. Section III illustrates the case study and describes the main sources of data used by the framework. In Section IV, the methodology used to estimate the rainfall is specified. Section V is devoted to some experimental results and discussion. Finally, Section VI concludes this article and shows some interesting future developments.

II. RELATED WORKS

The term “weather nowcasting” refers to weather forecasts concerning the near-future, typically a few hours, by using data coming from radars, satellites, and other sources, and usually, it is adopted to prevent many risks, such as landslides and floods. This field of research shares similar techniques and data sets with the task of rainfall estimation; therefore, we decided to analyze also some works concerning this field of research in the first part of this section.

Schroeter [8], similar to our work, also integrates input data coming from radars, RGs, and satellites and uses artificial neural networks (ANNs) as a forecasting method. Their experiments are conducted on real data concerning Australia and the integration of the data is necessary because, in this country, radar coverage is not optimal, particularly in regional areas. The experimental results show that their method overestimates the rainfall. In [9], an approach based on neural networks that keep track of spatiotemporal relationships is proposed to cope with the problem of rainfall nowcasting. However, only data provided by radars are considered. In [10], a hybrid approach based on recurrent neural networks and support vector machine (SVM) is used to provide rainfall forecasts from typical meteorological parameters, such as humidity, pressure, and temperature. An interesting review of the field of rainfall prediction can be found in [11].

Other works based on the ensemble paradigm include the work in [12], which, similar to our work, employs a probabilistic ensemble and merges two sources of data (i.e., rain gauges and radar) even if the aim of this work is to develop a run-off analysis. Afterward, a blending technique is applied to the results of the runoff hydrologic models to determine a single runoff hydrograph. Experimental results show that the hydrologic models are accurate and can help to make more effective decisions in the flood warning. Frei and Isotta [13] define a technique for deriving a probabilistic spatial analysis of daily precipitation from rain gauges. The final model represents an ensemble of possible fields, conditional on the observations, which can be explained as a Bayesian predictive distribution measuring the uncertainty due to the data sampling from the station network. An evaluation of a real case study, located in the European Alps, proves the capability of the approach in providing accurate predictions for a hydrological partitioning of the region. The work in [14] proposes an interesting study of the daily precipitations for Australia and several regions of South and East Asia, based only on high-resolution gauges. Basically, the adopted model can be figured out as a mean of the analyses generated for each source. The authors highlight how the ensemble approach outperforms the single members composing the model in terms of global accuracy. Moreover, the proposed model is also able to capture additional information from different precipitation products. Both the last two works exploit an ensemble scheme to provide more accurate predictions, proving the capability of ensemble methods to ensure good results also in a rainfall estimate scenario. However, different from our work, the adopted combination strategies are quite simple, and a combination of heterogeneous data sources is not considered.

The rest of this section is devoted to the analysis of works specifically designed for rainfall estimation. An extensive survey on these types of work can be found in [15]. For the same Italian region studied in our work, Calabria, Chiara Valloti et al. [16] studied the performance of three recently developed satellite-based products, i.e., IMERG, SM2RASC, and a clever combination of SM2RASC and IMERG using as a benchmark both RG only data and the integrated RG-radar product. Experiments permit to establish that IMERG has good performance at time resolutions higher than 6 h, and the combination of IMERG and SM2RASC obtains a higher quality satellite rainfall product. Most of the other approaches integrate data from different sources, i.e., satellite channels and radars. Some of them are based on the identification of suitable models that exploit the relation between optical and microphysical properties of clouds and use the data to find the appropriate parameters for these models [17], [18]. Other works individuate the models by using statistical techniques [19]–[21]. For instance, Bayesian estimation is used in [22] in order to provide precipitation
estimations based on satellite multispectral data; reference estimates are provided by methods that use radar data as input. Verdin et al. [23] also adopt Bayesian estimation in order to estimate the parameters of the model; their system integrates RG observations and satellite data and adopts an interpolation technique based on the Kriging method.

All these techniques are able to provide interesting results, but they require a rather delicate phase of parameters estimation of the particular model; therefore, as a side effect, usually, their flexibility and effectiveness tend to be hampered.

As the relations between sensors data, cloud properties, and rainfall estimates are highly nonlinear, more flexible approaches based on ML techniques have been investigated recently. For instance, the problem of detecting convective events and closely related rainy areas is addressed in [24] by using ANNs combined with support vector machines. Data sets are obtained by processing data coming from optical channels of the multispectral instrument onboard of Meteosat Second Generation (MSG) satellites; different from our work, RG measures are used only as a reference but not in the training phase of the algorithm. Sehad et al. [25] propose an approach to rainfall estimation based on SVMs; the input data are integrated from multispectral channels on MSG; and two models are developed for daytime and nighttime respectively. Results are compared to similar approaches based on ANNs, and random forest (RF) and RGs are used only to validate the approach. Another approach based on ANNs is described in [26]; in this work, given as an image matrix, radar data are used as reference in detecting rainy pixels. Kuhnlein et al. [27] also adopt the ensemble paradigm and, in particular, employ RFs to infer rainfall rates from data coming from multispectral channels on MSG satellites.

In [28], a hybrid architecture that combines support vector regression (SVR) models, genetic programming, and recurrent networks is presented. The experimental results, performed on a real data set concerning the typhoon season in northern Taiwan, exhibit good performance in estimating the height of the rainfall. Backpropagation neural networks are used in [29] to combine data coming from multispectral channels on MSG satellites and parameters usually considered in numerical weather predictions. Rainfall rates estimated from the radars are used in the training phase of the neural network. Deep neural networks are used to improve rainfall rates estimation using only radar data in [30] and [31].

Finally, in [32], different data mining techniques are compared on the problem of rainfall estimation from multispectral satellite data. Techniques considered include RF, neural networks, and support vector machines. Experiments show that no particular algorithm performed dramatically better than the others; the authors conclude that further research is necessary to investigate whether different base learners could improve the results.

Our approach is also similar to some of the analyzed works on the ensemble paradigm; however, we do not rely on a single data source, as do most of the works present in the literature, but our approach integrates information coming from different sources, i.e., radars, satellites, and RGs. In addition, as the classes in this problem are intrinsically unbalanced, we also perform an undersampling during the training phase, which it is not used in the other works.

III. CASE STUDY: RAINFALL ESTIMATION IN CALABRIA

In this section, the peculiarities of the Calabria region and the main characteristics of the three sources of data integrated to estimate the rainfall events are described.

A. Data Description

Calabria covers an area of 15,000 km². This region exhibits high climatic variability [33], mainly due to its particular orography (i.e., the proximity of mountains and seas) and to the influence of the Mediterranean Sea. Calabria is characterized by the presence of small and very small basins that may be prone to landslides and flash floods during localized rainfall [34], [35]. Thus, an accurate spatial rainfall field is necessary for hydrological impact studies and for a correct analysis of hydrological scenarios producing floods and landslides affecting this fragile territory [36]. For these reasons, RG, weather radar, and MSG data collected during 2016 for Calabria will be used to test the framework developed in this work.

In particular, the Calabrian DCP supplies RG data, extracted from a real-time monitoring system consisting of a network of 156 telemetered sensors with an average distance of about 10 km. These data consist of precipitation heights measured in mm sampled every minute.

Radar data are supplied by the DCP, by exploiting the Italian meteorological radar network (20 weather radars spread over the whole Italian territory). Data are collected in near real time and processed by merging high-resolution volumetric data using the methodology described in [37]. The final data have a time resolution of 10 min over a grid with a spatial resolution of 1 km and include Constant Altitude Plan Position Indicator (CAPPI) that gives a horizontal cross section of reflectivity at 2000, 3000, and 5000 m above sea level (a.s.l.); vertical maximum intensity (VMI) that represents the maximum reflectivity value present on every point’s vertical axis; and the surface rain intensity (SRI) that estimates the ground rain rate. The SRI product is obtained applying the Marshall–Palmer reflectivity-rainfall (Z-R) relationship to the lowest radar beam [38]. The study area is covered by two C-band weather radars, and their range is about 200 km (see Fig. 1).

The Meteosat Second Generation (MSG) data are provided by the European Organization for the Exploitation of Meteorological Satellites (EUMETSAT). The Spinning Enhanced Visible and Infrared Imager (SEVIRI), onboard the geostationary MSG satellite, supplies detailed images of the full Earth disk at 12 different wavelengths and monitors the dynamic evolution of cloud structures at a high temporal resolution due to the rapid scan service (RSS), which provides an image every 5 min [39]. These characteristics allow the detection of rapidly developing high impact weather. Moreover, data from different channels correspond to different physical properties of the observed cloudy structures. For example, in the thermal infrared band (10–12 μm), satellites supply indications on
Fig. 1. Map of Calabria, projection system UTM WGS84, zone 33N. The points represent the RG network, while the large dashed circles represent the radar ranges (the location of the Calabrian radar is indicated by the solid triangle).

the temperature of the cloudy area, which is related to the cloud height and to the convection development. The spatial resolution for the region considered in this work is about 4 km.

IV. METHODOLOGY

This section describes the methodology proposed to estimate the rainfall in a specific zone exploiting an ML-based approach.

In Fig. 2, the overall learning and evaluation process, composed of three main phases (i.e., information retrieval, ML, and evaluation), is sketched. Information retrieval focuses on gathering the data required for the analysis. In this phase, different types of information, from several data sources, are extracted and integrated. Especially, a data source connector is used to establish the connection with a specific data source; then, the gathered data are provided as input for the data wrapper that combines these data in a single view suitable for the next analysis phase. Raw data are stored in the knowledge base (KB), which is exploited for the data exchange among the framework components.

In the ML phase, raw data are preprocessed to make them suitable for the analysis, and an undersampling strategy is adopted to address the class unbalanced problem. Then, a rainfall estimation model can be trained from the preprocessed data. To this aim, in this work, we introduce a novel metaensemble probabilistic classifier (named HPEC in the figure) and described in Section IV-C. However, the architecture is modular, and also another different estimation model could also be adopted.

In the final phase, i.e., evaluation, the rainfall estimations are computed for a set of preprocessed data by exploiting the trained model. This phase can be performed on both: 1) ungauged points (in a real usage scenario) in order to estimate the severity class of these points and 2) a separated set of training data (i.e., not used in the learning phase). For this latter case, how specified in the experimental section, we know the real class (as an RG is present); however, this value is removed in order to obtain the estimated class, and it is used only to compute the performance measures also reported in the experiments.

In the following, the preprocessing phase (the way in which the information extracted by several data sources is combined) and the proposed ensemble-based approach are detailed.

A. Data Preprocessing

One of the main novelties of the approach is the integration of three main sources of data to better estimate rainfall events. However, the integration needs to overcome the issues concerning the heterogeneity of the data, so some preprocessing operations have to be performed to adjust the different scales both in terms of time and space.

A 30-min temporal sampling of the measurements was deemed appropriate for the purposes of this article, considering an acceptable balance between the need for a high temporal resolution and the need to reduce the statistical noise of the data (as pointed out in [40]); therefore, the RGs and the SRI data were cumulated every 30 min. Furthermore, as, in many cases, near points exhibit related rain conditions, it is useful to take into account the distance among the RGs. Thus, for every point, the coordinates of the four nearest points containing an RG, together with the distance, are considered.

To summarize, for every point in which an RG is present, for a 30-min time step, 35 features were extracted (as also illustrated in Table I), as detailed in the following.

1) From the Radars (5 Features): SRI, cumulated over 30 min, VMI, and three values of CAPPI (horizontal cross section of reflectivity at 2000, 3000, and 5000 m a.s.l.); the last value was taken for all these four features.

2) From the MSG Satellites (11 Features): The last value of the 11 Meteosat channels (excluding the high-resolution visible channel number 12).

3) From the RGs (16 Features): The coordinates of the four nearest points containing an RG, together with the distance and the value measured by the RG.
TABLE I
FEATURES EXTRACTED FROM THE THREE SOURCES OF DATA: RADAR, SATELLITE, AND RGs (i = 1, . . . , 4)

<table>
<thead>
<tr>
<th>Source</th>
<th>Name</th>
<th>Time res.</th>
<th>Space res.</th>
<th>Unit of meas.</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radar</td>
<td>SRI</td>
<td>10 min.</td>
<td>1 km</td>
<td>mm/h</td>
<td>Surface rainfall intensity</td>
</tr>
<tr>
<td></td>
<td>VMI</td>
<td>10 min.</td>
<td>1 km</td>
<td>dBZ</td>
<td>Maximum reflectivity on the vertical</td>
</tr>
<tr>
<td></td>
<td>CAPPI2000</td>
<td>10 min.</td>
<td>1 km</td>
<td>dBZ</td>
<td>Reflectivity at the heights of 2000 m</td>
</tr>
<tr>
<td></td>
<td>CAPPI3000</td>
<td>10 min.</td>
<td>1 km</td>
<td>dBZ</td>
<td>Reflectivity at the heights of 3000 m</td>
</tr>
<tr>
<td></td>
<td>CAPPI5000</td>
<td>10 min.</td>
<td>1 km</td>
<td>dBZ</td>
<td>Reflectivity at the heights of 5000 m</td>
</tr>
<tr>
<td>MSG</td>
<td>Ch1</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>0.635µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch2</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>0.81µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch3</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>1.64µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch4</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>3.9µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch5</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>6.25µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch6</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>7.35µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch7</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>8.7µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch8</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>9.66µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch9</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>10.8µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch10</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>12µm channel brightness temperature</td>
</tr>
<tr>
<td></td>
<td>Ch11</td>
<td>5 min.</td>
<td>4 km</td>
<td>K</td>
<td>13.4µm channel brightness temperature</td>
</tr>
<tr>
<td>Rain gauge</td>
<td>$x_i$</td>
<td>-</td>
<td>punctual</td>
<td>m</td>
<td>$x$ coordinate of the $i^{th}$ rain gauge</td>
</tr>
<tr>
<td></td>
<td>$y_i$</td>
<td>-</td>
<td>punctual</td>
<td>m</td>
<td>$y$ coordinate of the $i^{th}$ rain gauge</td>
</tr>
<tr>
<td></td>
<td>dist</td>
<td>-</td>
<td>continuous</td>
<td>m</td>
<td>distance from the $i^{th}$ rain gauge</td>
</tr>
<tr>
<td></td>
<td>rainfall</td>
<td>1 min</td>
<td>punctual</td>
<td>mm</td>
<td>mm of precipitation</td>
</tr>
</tbody>
</table>

4) **Other Data (Three Features):** Longitude and latitude of the point and the month in which the data are detected.

It is important to remark that different spatial resolutions have been used in the data fusion process (respectively, 1 km for the radar and 4 km for the MSG satellite); in practice, the features, respectively coming from of the resolution cell (pixel) of the satellite or of the radar, are determined by the point in which the RG falls.

The final data set covers a period concerning the second half of 2016 in Calabria. After the phase of undersampling and preprocessing, it consists of 117,600 tuples and 35 features. Each tuple represents an observation for a predetermined period of time of 30 min, in a point of space corresponding to one of the 156 RGs in Calabria. The class to be estimated is measured by the RGs, and consider the mm of rain fell in the considered range of 30 min and is discretized into five classes according to these ranges: [0 − 0.5, 0.5 − 2.5, 2.5 − 7.5, 7.5 − 15, 15 − ]. The numbers of tuples for each class are, respectively, 94,080, 18,514, 4,221, 654, and 131. The correct classification of the latter two classes is particularly important because they represent heavy rainfall events, which must be handled adequately. However, the number of tuples belonging to these two classes is really unbalanced as the ratio between each of them and the majority class (0 − 0.5, named in the following no-rain for the sake of simplicity) is very low, and therefore, correctly classifying these two rare classes of events is a really challenging problem.

**B. Undersampling Strategy**

After the integration of the three data sources, i.e., RG data, weather radar, and MSG data, a sampling strategy must be adopted to avoid the class unbalance issue. In the class unbalance problem [41], the minority classes are overcome by the numerosness of the majority class. In the literature, different strategies are proposed to tackle this problem; in particular, the techniques based on undersampling obtain good results in terms of accuracy, while oversampling the other classes usually causes overfitting. Therefore, we adopt an undersampling strategy [42] operating only on the no-rain class, while the other four classes, representing different levels of rain, are not affected by the method. A random uniform undersampling strategy is adopted, which operates on two levels: first, only temporal periods presenting all the points without rain events are chosen; then, always uniformly, a random number of spatial points are removed from this period. In order to avoid loss of information, nothing is done in days presenting rain and no-rain points.

**C. Ensemble-Based Approach**

In our framework, the rainfall estimation problem is addressed as a classification task. A classifier permits to divide the data into predefined categories (also called classes). Frequently, classifiers are also used to predict unknown categories for new unseen instances.

Formally, let $S = \{(x_i, y_i) | i = 1, \ldots, N\}$ be a training set where $x_i$, called example or tuple or instance, is an attribute vector with $m$ attributes and $y_i$ is the class label associated with $x_i$, where $x_i \in \{L_1, \ldots, L_C\}$ and $C$ is the number of classes. A classifier, given a new example, has the task to assign the class label for it, i.e., the task consists of computing a function $h(x_i)$ that is able to estimate $y_i^*$ (with $y_i^* \approx y_i$).

Ensemble [7], [43] is a learning paradigm where multiple base learners are trained for the same task by a learning algorithm, and the classifications of the component learners are combined for dealing with new unseen instances. In our framework, a set of classifiers is adopted as base learners.

Formally, as shown in Fig. 3, ensemble techniques build $S$ classifiers $T_1, \ldots, T_S$, each one trained on a different sampling of the training set (or also on differently weighted tuples of
the same training set or adopting different learning algorithms always on the same training set); then, they are combined according to a suitable combination strategy to classify the test set. Basically, given as input the classifications of the base classifiers $T_1, \ldots, T_r$, ensemble learning techniques allow combining them and computing a function $h^*$ that is able to produce the final classification.

In the literature, three standard combination strategies have been widely used: boosting, Bootstrap aggregation (bagging), and stacking.

Boosting was introduced by Schapire [44] and Freund [45] to improve the performance of any “weak” learning algorithm, i.e., an algorithm that “generates classifiers that need only be a little bit better than random guessing” [45]. The boosting algorithm, called AdaBoost, adaptively changes the distribution of the training set according to how difficult each example is to classify.

Basically, in bagging-based approaches [7], different subsets of the training data (extracted via a bootstrap resampling strategy) are used to train the base learners, while the final assignment is computed via a simple voting scheme.

Stacking [46] (stacked generalization) is an effective ensemble-based approach able to exploit the output of several classifiers to learn a more accurate metalearner. The whole training set is used to learn each single base model. Basically, the algorithm uses the trained models to build a stacked view, i.e., a table, in which each row corresponds to the classification of each base model for the corresponding tuple of the training data set; therefore, each column contains the assignment of each classifier. Finally, this view is used to train a metalearner in order to compute the final classification. Alternatively, the class probabilities of the same classifiers can be directly used to train the metalearner. In our approach, we adopt this latter strategy.

RF [47] is an efficient and particularly accurate ensemble-based technique. This algorithm combines simultaneously two different strategies: a bagging algorithm and a random selection of the features. Especially, the bagging approach is applied to a set of tree-based classifiers (base models). The main difference with respect to a simple bagging method relies on the building procedure of the decision trees, which are trained and evaluated only on a randomly chosen subset of the features.

In our methodology, after the preprocessing and undersampling steps, an HPEC is adopted to learn a model able to estimate the rainfall events. The source code of HPEC, used to run the experimental results shown in Section V, is available at https://github.com/massimo-guarascio/ml-rainfall.

Although the idea of combining different learners in a hierarchical way is not new in itself, to the best of our knowledge, our specific hierarchical model has not been previously used to tackle the rainfall estimation problem.

Usually, when the number of examples for the minority classes is low in comparison with the majority class, stacking-based techniques behave better, as they avoid the overfitting problem typical in unbalanced data sets. Therefore, we adopted a stacking method for HPEC, which follows the architecture reported in Fig. 4. As a base learner, in the first stage, we adopt RFs (note that an RF is also an ensemble), as this technique exhibits good performance in unbalanced scenarios, reducing the problem of the overfitting, as different subsets of features are exploited in the training phase.

Especially, our approach exploits a two-level ensemble classifier: 1) in the first level, a set of ensembles (i.e., the RF classifiers) are trained on the same data set, but initialized with different random seeds, in order to vary the feature subset generation during the learning of the decision trees composing the forest and 2) in the second level, a probabilistic metalearner is used to combine the estimates provided by the first level classifiers according to a stacking schema [46]. In more detail, their estimates are combined in a stacked view, in which each row contains an estimate (i.e., a vector composed of the class probabilities, provided by each base model) for the class of the tuple $i$ of the training data set. This view is provided as input for a probabilistic Bayesian model. Finally, the output of the metalearner is the estimate of the class of the rainfall event, obtained on the basis of the probabilities provided by the base models.

V. EXPERIMENTAL RESULTS

In order to assess the quality of our approach in estimating rainfall, different experiments on the real data concerning Calabria are conducted. First, different ensemble-based techniques (RF, boosting, and HPEC) are compared. In addition, these ensemble algorithms are also compared with the decision tree algorithm and with the support vector regression model, which has been successfully used in the field of rainfall forecasting.
Then, the ensemble approach is compared with the baseline method (Kriging with external drift), largely used and well-recognized in the field of rainfall estimation. Finally, the different contributions of neighboring RGs, satellites, and radar measures are studied.

The ensemble-based algorithms, the decision tree, and the SVR model, adopted in this article, are based on the well-known scikit-learn ML implementation.\(^1\) If not differently specified, the algorithms were run using standard parameters. No tuning of the parameters was conducted. As for the KED method, we used the RG data as the primary variable and the radar data as the auxiliary information. The KED interpolation is performed by using the “autokrig” method described in [48] and implemented in the Automap and Gstat libraries of the statistical software R. Using this method, the theoretical variogram is automatically determined by picking the best fitting model. This procedure results in fully automated, and it allows, in near real-time, the estimation of the areal rainfall field over a \(1 \times 1 \text{ km}^2\) spatial grid, with a time resolution of 10 min.

All the algorithms were trained on a training set composed of 2/3 of the original data set and then evaluated on the test set, consisting of 1/3 of the original data set. In practice, for each period of time, 2/3 of the observation points (RGs) were randomly chosen from the original data set, and they form the training set, while the remaining points will constitute the test set (and are excluded also for the interpolation method of Kriging). The original data are continuous; however, our classification approach needs discretized classes to work, and in addition, we are interested in retrieving the fine spatial structure of the precipitation field in order to correctly interpret the level of hazard for a given area (and not in the estimating the high-resolution value of rainfall). Therefore, the HPEC classification process is conducted after discretization of the original data into five classes, as described in Section IV-A.

For all the measures, the Friedman test is verified, and consequently, the differences among the algorithms are significant. For all the measures, the Friedman test is verified, and consequently, the differences among the algorithms are significant. Therefore, the null hypothesis is rejected, and then, in the following, we analyze the rankings and the post hoc test for the most important measures for our particular application, i.e., FAR, POD, and MSE (see Table II) and Recall and F-measure for the minority (and presenting a high-intensity of rainfall) classes 4 and 5 are shown.

All the experiments were averaged over 30 runs. We adopt metrics taking into account the rarity of the minority classes, in order to avoid the problem of overestimating the accuracy of a classifier to recognize the instances of these classes correctly. Notably, true positive (TP), false positive (FP), true negative (TN), and false negative (FN) can be easily computed from the confusion matrix.

Therefore, in addition to the well-known metrics of Precision and Recall (in the field of rainfall estimation, usually named POD, i.e., probability of detection), computed, respectively, as Precision = (TP/FN + TP) and Recall = (TP/FN + TP), we adopted some measures, deriving from these metrics, largely used in the field of rainfall estimation [49], i.e., the false-alarm ratio (FAR), computed as FAR = (FP)/(TP + FP), the critical success index (CSI), computed as CSI = (TP)/(TP + FP + FN), and the mean square error (MSE), computed as MSE = \((1/n)\sum_{i=1}^{n}(y^{(i)} - \tilde{y}^{(i)})^2\), where \(n\) is the number of points and \(y^{(i)}\) and \(\tilde{y}^{(i)}\) are, respectively, the real and the estimated class. Finally, we also considered F-measure, i.e., the weighted harmonic mean of precision and recall (or POD), computed only for the minority classes (4 and 5), which regard intense rainfall events.

### A. Comparison of Ensemble-Based Techniques

We performed the Friedman test for all the evaluation measures (columns) of Tables II and III, while the Nemenyi is adopted as post hoc test, as suggested in [50].

Table II reports the values of CSI (higher is better), FAR (lower is better), POD (higher is better), and MSE (lower is better) for the five algorithms, while, in Table III, Precision, Recall, and F-measure for the minority (and presenting a high-intensity of rainfall) classes 4 and 5 are shown.

For all the measures, the Friedman test is verified, and consequently, the differences among the algorithms are significant. Therefore, the null hypothesis is rejected, and then, in the following, we analyze the rankings and the post hoc test for the most important measures for our particular application, i.e., FAR, POD, and MSE (see Table II) and Recall and F-Measure (see Table III) for the minority classes.

In terms of POD, the test indicates that HPEC is significantly better than the other approaches. No significant differences are reported between SVR and decision tree and also for boosting and RF.

As for the mean-square error (MSE), according to the significance test, the RF algorithm is significantly better than the other ones, while HPEC is not significantly different from the other algorithms.

As for the F-measure, for the minority class 4, both in terms of Recall and F-measure, HPEC is significantly better than all the other approaches. On the contrary, RF and boosting are not significantly different, and in the same way, SVR and

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\(^1\)http://scikit-learn.org/stable/
TABLE IV
CSI, FAR, POD, AND MSE FOR THE KRIGING, RF, AND HPEC. THE VALUES IN BOLD (LIGHT GRAY) ARE SIGNIFICANTLY BETTER (WORSE) THAN THE KRIGING METHOD

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>CSI</th>
<th>FAR</th>
<th>POD</th>
<th>MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kriging</td>
<td>0.40 ± 0.010</td>
<td>0.49 ± 0.018</td>
<td>0.48 ± 0.013</td>
<td>0.15 ± 0.002</td>
</tr>
<tr>
<td>Random Forest</td>
<td>0.43 ± 0.010</td>
<td>0.31 ± 0.024</td>
<td>0.49 ± 0.011</td>
<td>0.09 ± 0.002</td>
</tr>
<tr>
<td>HPEC</td>
<td>0.44 ± 0.011</td>
<td>0.46 ± 0.016</td>
<td>0.58 ± 0.016</td>
<td>0.11 ± 0.002</td>
</tr>
</tbody>
</table>

TABLE V
PRECISION, RECALL, AND F-MEASURE FOR THE KRIGING, RF, AND HPEC FOR THE MINORITY CLASSES 4 AND 5. THE VALUES IN BOLD (LIGHT GRAY) ARE SIGNIFICANTLY BETTER (WORSE) THAN THE KRIGING METHOD

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Precision</th>
<th>Recall</th>
<th>F-measure</th>
</tr>
</thead>
<tbody>
<tr>
<td>Class 4</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Kriging</td>
<td>0.37 ± 0.042</td>
<td>0.20 ± 0.026</td>
<td>0.26 ± 0.031</td>
</tr>
<tr>
<td>Random Forest</td>
<td>0.47 ± 0.067</td>
<td>0.09 ± 0.011</td>
<td>0.15 ± 0.020</td>
</tr>
<tr>
<td>HPEC</td>
<td>0.24 ± 0.034</td>
<td>0.28 ± 0.030</td>
<td>0.26 ± 0.027</td>
</tr>
<tr>
<td>Class 5</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Kriging</td>
<td>0.45 ± 0.078</td>
<td>0.32 ± 0.059</td>
<td>0.38 ± 0.062</td>
</tr>
<tr>
<td>Random Forest</td>
<td>0.68 ± 0.101</td>
<td>0.23 ± 0.042</td>
<td>0.35 ± 0.037</td>
</tr>
<tr>
<td>HPEC</td>
<td>0.33 ± 0.062</td>
<td>0.40 ± 0.066</td>
<td>0.36 ± 0.057</td>
</tr>
</tbody>
</table>

decision tree are not significantly different. Finally, for class 5, HPEC is significantly better than all the other algorithms for the recall measure, while the ensemble-based algorithms overcome the other algorithms for the F-measure, but they are not significantly different among themselves. Therefore, by considering that we are particularly interested in detecting a larger number of heavy rainfall events (class 4 and 5), HPEC appears to be a good choice.

B. Comparison of Ensemble-Based Algorithms and Kriging

This section aims to evaluate whether ensemble-based algorithms improve the performance in comparison with largely used traditional algorithms designed by experts of the domain, as the Kriging algorithm. More in detail, the adopted algorithm is Kriging with external drift (KED), using the RG and the radar data, respectively, as primary and secondary variables.

The significance of the differences between Kriging and each ensemble algorithm is evaluated by using the Wilcoxon signed-ranked test [confidence level equal to 0.95 ($\alpha = 0.05$)]. This test is conducted both for Kriging versus RF and Kriging versus HPEC, as we are mainly interested in the comparison with the Kriging algorithm. The values that are significantly better are reported in bold, while the values that are significantly worst are reported in light gray.

Table IV reports, for the three algorithms, the values of CSI, FAR, POD, and MSE, while Table V reports Precision, Recall, and F-measure for the minority (and high-rate rainfall) classes 4 and 5. For all the measures, the ensemble-based algorithms perform significantly better (see Table IV). In particular, HPEC reaches a high value for the POD measure (0.58).

As for the minority classes, in spite of having a worse precision, HPEC exhibits a better recall. In addition, by considering the F-measure, there are no significant differences between Kriging and HPEC both for classes 4 and 5, while the RF algorithm behaves considerably worse. However, the MSE is considerably better for the ensemble-based techniques in comparison with KED. Then, the misclassification regards, in many cases, classes not so dissimilar for the amount of rainfall, i.e., a rainfall of class 4 could be assigned to class 3 or 5.

The results of this section suggest that a clever combination of Kriging and ML algorithms could further improve the capacity of the framework to detect heavy rainfall events.

An example of the differences in reconstructing the rainfall is shown in Fig. 5, respectively, (a) for the HPEC and (b) for KED. We would like to point out that this figure gives just a qualitative idea of the behavior of the two techniques for a significant event. We choose a very rainy event outside of the training period considered (November 6, 2017), in which three RGs registered their annual maximum of rainfall (about 42.4 mm for an hour). In order to compare the results, we consider the rain cumulated every 30 min, and we discretize the estimate of the Kriging method on the same classes considered for the ML approach. From this figure, it seems that the HPEC approach gives better detail of the rainfall events; however, further investigations should be conducted to draw a conclusion. For a more accurate comparison, it would be better to refer to the results reported in the previous tables.

C. Effect of Integrating RG, Satellite, and Radar Measurements

Similar to other works [8], [25], in our framework data coming from RGs, satellites, and radars are integrated in order to classify rainfall events better. In this section, we want to investigate the effect of this integration, by understanding whether all the three types of measurement are necessary to the classification. To this aim, by using the HPEC, we run three different suites of experiments by excluding, for each suite, one of the three types of measurement.
respectively). As for the last two classes, representing intense rainfall events, the difference between the Kriging method and HPEC is not significant (in terms of F-measure) although HPEC is computationally more efficient.

Indeed, the complexity of the Kriging method is cubic in the number of the samples [51], which makes the procedure really expensive from the computational point of view, when a large number of points are analyzed. On the contrary, the ML algorithms (i.e., RF) exhibit a quadratic complexity. Moreover, ensemble methods are highly scalable and parallelizable. Therefore, we believe that our approach has some relevant advantages in this field of application.

In addition, by analyzing the effect of the integration of the different sources of data, it is evident that all the data sources contribute to the good performance of the technique. In particular, by removing the RG information, the performance of the algorithm worsens the sensibly for all the measures. In the cases of the removal of one of the other two types of data, the degradation is less evident; however, the lowest value (0.11) of the MSE is obtained when all the data are used, which confirms the utility in using all the sources of data.

The benefit derived from the integration of the three sources is also confirmed by the F-measure in Table VII.

VI. CONCLUSION AND DISCUSSION

An ML-based approach for the spatial rainfall field estimation has been defined. By integrating heterogeneous data sources, such as RGs, radars, and satellites, this methodology permits estimation of the rainfall, where RGs are not present, also exploiting the spatial pattern recognition ensured by radars and satellites. After a phase of preprocessing, a random uniform undersampling strategy is adopted, and finally, an HPEC permits the model used to be built to estimate the severity of the rainfall events. This ensemble is based on two levels: in the first level, a set of RF classifiers are trained, while, in the second level, a probabilistic metalearner is used to combine the estimated probabilities provided by the base classifiers according to a stacking schema.

Experimental results conducted on real data provided by the Department of Civil Protection show significant improvements in comparison with Kriging with external drift, a largely used and well-recognized method in the field of rainfall estimation. In particular, the ensemble method exhibits a better capacity in detecting the rainfall events. Indeed, both the POD (0.58) and the MSE (0.11) measures obtained by HPEC are significantly better than the values obtained by KED (0.48 and 0.15, respectively). As for the last two classes, representing intense rainfall events, the difference between the Kriging method and HPEC is not significant (in terms of F-measure) although HPEC is computationally more efficient.

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As future work, we plan to validate the method on a larger time interval, in order to consider effects due to seasonal and yearly variability, also considering the possibility of incrementally building the flexible ensemble model with the new data. In addition, we want to evaluate the effectiveness of the algorithm in individuate highly localized heavy precipitation events, also by adopting time series analysis to analyze the individual contributions of the different features for radar and Meteosat.

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