Training Distributed GP Ensemble with a Selective Algorithm based on Clustering and Pruning for Pattern Classification

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Index terms: data mining, genetic programming, classification, clustering, ensemble, boosting.

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Abstract

A boosting algorithm based on cellular genetic programming to build an ensemble of predictors is proposed. The method evolves a population of trees for a fixed number of rounds and, after each round, it chooses the predictors to include into the ensemble by applying a clustering algorithm to the population of classifiers. Clustering the population allows the selection of the most diverse and fittest trees that best contribute to improve classification accuracy. The method proposed runs on a distributed hybrid environment that combines the island and cellular models of parallel genetic programming. The combination of the two models provides an efficient implementation of distributed GP, and, at the same time, the generation of low sized and accurate decision trees. The large amount of memory required to store the ensemble makes the method heavy to deploy. The paper shows that, by applying suitable pruning strategies, it is possible to select a subset of the classifiers without increasing misclassification errors; indeed, for some data sets, up to 30% of pruning, ensemble accuracy increases. Experimental results show that the combination of clustering and pruning enhances classification accuracy of the ensemble approach.

1 Introduction

Ensemble learning algorithms have captured an increasing interest in the research community because of their capability of improving the classification accuracy of any single classifier. An ensemble of classifiers is constituted by a set of predictors that, instead of yielding their individual decisions to classify new examples, combine them together by adopting some strategy [4, 5, 6, 12, 19]. It has been pointed out that the boost in accuracy is tightly related with the diversity of the classifiers [12, 22]. Two classifiers are defined to be diverse if they make different incorrect predictions on new data points. Several approaches for building ensembles satisfying the diversity demand have been proposed. The *AdaBoost* algorithm introduced by Freund and Schapire [19] showed to be efficacious at generating different classifiers. It guides the underlying learning algorithm to focus on harder examples by adaptively changing the distributions of the training set on the base of the performance of previous classifiers.

The combination of Genetic Programming (GP) [21] and ensemble techniques has been receiving a lot of attention because of the improvements that GP obtains when enriched with these methods [26, 25, 10, 17, 20, 23, 30].

It is worth pointing out that an advantage of using GP, not yet exploited, is that a population of predictors could be considered as an ensemble of predictors. This assumption would provide at the same time many and diverse classifiers. However, the size of a population generally is not small. Another problem could be the accuracy of some of the trees contained in the population. Taking all the individuals of a population at each generation is not a practical approach because of the resulting high number of predictors, possibly of low quality. A plausible proposal would be to use a clustering algorithm [13] to group individuals in the population that are similar with respect to a similarity measure and then take the representatives of these clusters. In this paper a distributed boosting cellular Genetic Programming classifier to build the ensemble of predictors is proposed. The algorithm, named *ClustBoostCGPC* (*Clustering Boost Cellular Genetic Programming Classifier*), runs on a distributed environment based on a hybrid model [2] that combines the island model with the cellular model. The island model enables an efficient implementation of distributed GP. On the other hand, the cellular model allows the generation of classifiers with better accuracy and reduced tree size. Each node of the network is considered as an island that contains a learning algorithm, based on cellular genetic programming, whose aim is to generate decision-tree predictors trained on the local data stored in the node. Every genetic program, however, though isolated, cooperates with the neighboring nodes by collaborating with the other learning components located on the network, and takes advantage of the cellular model by asynchronously exchanging the outermost individuals of the population.

ClustBoostCGPC constructs an ensemble of accurate and diverse classifiers by employing a clustering strategy to each subpopulation located on the nodes of the network. The strategy, at each boosting round, finds groups of individuals similar, with respect to a similarity measure, and then takes the individual of each cluster having the best fitness. This allows the selection, from each subpopulation, of the most dissimilar and fittest trees.

The main drawback of the approach proposed is that the size of the ensemble increases as the number of clusters and the nodes of the network increases. Thus we could ask if it is possible to discard some of these predictors and still obtain comparable accuracy. The paper shows that, by applying suitable pruning strategies, it is possible to select a subset of the classifiers without augmenting misclassification errors; indeed, up to 30% of pruning, ensemble accuracy increases. The main contributions of the paper can be summarized as follows.

ClustBoostCGPC is a distributed ensemble method that mixes a supervised classification method with an unsupervised clustering method to build an ensemble of predictors.

Clustering the population of classifiers revealed a successful approach. In fact the misclassification error rate of the ensemble sensibly diminishes when the ensemble is constituted by the best individuals in the clustered populations. The method is enriched with pruning strategies that allow the reduction of the size of the ensemble, and, more notably, to improve classification accuracy. This result agrees with the logical principle of Occam's razor that one should not make more assumptions than the minimum needed and choose, from a set of equivalent models, the simplest one.

The algorithm runs on a distributed environment. The distributed architecture gives significant advantages in flexibility, extensibility, and efficiency since each node of the network works with its local data, and communicates the local model computed with the other nodes to obtain the results.

To assess the effectiveness of the method, experiments on several data sets are presented and compared with other approaches when different sizes of the ensemble are used.

Three pruning strategies are presented and compared to analyze their influence on the ensemble accuracy. The combination of these strategies is then investigated with the aim of decreasing ensemble size and improving classification accuracy. Experimental results pointed out that the proposed approach is particularly effective since it reduces the misclassification error rate of the algorithm.

This paper is organized as follows. The next section reviews ensemble techniques. In Section 3 the algorithm *ClustBoostCGPC* and the software architecture used to run it are described. Section 4 describes the pruning strategies adopted to reduce the size of the ensemble. In section 5 the results of the method on some standard problems are presented. Section 7, finally, concludes the paper by giving a discussion of the approach and some final considerations.

2 Ensemble techniques

Let $S = \{(x_i, y_i) | i = 1, ..., N\}$ be a training set where x_i , called example or tuple or instance, is an attribute vector with m attributes and y_i is the class label associated with x_i . Let \mathcal{X} denote the set of tuples and \mathcal{Y} the set of class labels. Each attribute can be either discrete or continue. A predictor (classifier), given a new example, has the task to predict the class label for it.

Ensemble techniques [4, 5, 12, 28] build a number of predictors, each on a different training set, then combine them together to classify the test set. Boosting was introduced by Schapire [28]

and Freund [29] for boosting the performance of any "weak" learning algorithm, i.e. an algorithm that "generates classifiers which need only be a little bit better than random guessing" [29].

The boosting algorithm, called AdaBoost, adaptively changes the distribution of the training set depending on how difficult each example is to classify. Given the number T of trials (rounds) to execute, T weighted training sets S_1, S_2, \ldots, S_T are sequentially generated and T classifiers C^1, \ldots, C^T are built to compute a weak hypothesis $h_t : \mathcal{X} \to \mathcal{Y}$. Let w_i^t denote the weight of the example x_i at trial t. At the beginning $w_i^1 = 1/n$ for each x_i . At each round $t = 1, \ldots, T$, a weak learner C^t , whose error ϵ^t is bounded to a value strictly less than 1/2, is built and the weights of the next trial are obtained by multiplying the weight of the correctly classified examples by $\beta^t = \epsilon^t/(1 - \epsilon^t)$ and renormalizing the weights so that $\Sigma_i w_i^{t+1} = 1$. Thus "easy" examples get a lower weight, while "hard" examples, that tend to be misclassified, get higher weights. This induces AdaBoost to focus on examples that are hardest to classify. The boosted classifier gives the class label y that maximizes the sum of the weights of the weak hypotheses predicting that label, where the weight is defined as $ln(1/\beta^t)$.

Freund and Schapire [29] showed theoretically that AdaBoost can decrease the error of any weak learning algorithm and introduced two versions of the method, AdaBoost.M1 and AdaBoost.M2. AdaBoost.M1, when the number of classes is two, requires that the prediction be slightly better than random guessing. However, when the number of classes is more than 2, a more sophisticated error-measure, called *pseudo-loss*, is introduced. In this paper we use the AdaBoost.M1 version.

Proposals to combine *Genetic Programming* and ensemble techniques can be found in [26, 25, 10, 17, 20, 23, 30].

In particular, BoostCGPC (Boost Cellular Genetic Programming Classifier) [17] implements the AdaBoost.M1 boosting algorithm of Freund and Shapire [19] on a parallel computer by using the algorithm CGPC (Cellular Genetic Programming for data classification) [15] as base classifier. Given a training set S of size N and the number P of processors used to run the algorithm, BoostCGPC partitions the population of classifiers in P subpopulations, creates P subsets of tuples of size n < N by uniformly sampling instances from S with replacement, and builds an ensemble of classification trees by choosing from each subpopulation the individual having the best fitness. In the next section the algorithm ClustBoostCGPC is presented and the main differences with BoostCGPC are outlined.

3 ClustBoostCGPC

In this section the description of the algorithm ClustBoostCGPC is given. The method builds an ensemble of classifiers by using, analogously to BoostCGPC, at each round of the boosting procedure, the algorithm CGPC (*Cellular Genetic Programming for data classification*) [15] to create a population of predictors. However, instead of choosing, like BoostCGPC, from each subpopulation the individual having the best fitness, it finds k groups of individuals similar with respect to a similarity measure by employing the clustering algorithm k-means and then takes the individual of each cluster having the best fitness. Before giving a detailed outline of the approach proposed, a brief review of the CGPC and k-means methods is provided.

3.1 The CGPC algorithm

Genetic programming can be used to inductively generate a GP classifier as a decision tree for the task of data classification [21]. Decision trees, in fact, can be interpreted as composition of functions where the function set is the set of attribute tests and the terminal set are the classes. The function set can be obtained by converting each attribute into an attribute-test function. For each attribute A, if $A_1, \ldots A_n$ are the possible values A can assume, the corresponding attributetest function f_A has arity n and if the value of A is A_i then $f_A(A_1, \ldots A_n) = A_i$. When a tuple has to be evaluated, the function at the root of the tree tests the corresponding attribute and then executes the argument that outcomes from the test. If the argument is a terminal, then the class name for that tuple is returned, otherwise the new function is executed. Suppose to have a data set with two class labels X and Y, and attribute set $\{A(a_1, a_2, a_3), B(b_1, b_2), C(c_1, c_2), D(d_1, d_2)\}$, where $a_i, 1 \le i \le 3, b_j, c_j, d_j, j = 1, 2$ is the set of possible values A, B, C, D respectively can assume. Then the terminal set is $\mathcal{T} = \{X, Y\}$ and the function set $\mathcal{F} = \{f_A(a_1, a_2, a_3), f_B(b_1, b_2), f_C(c_1, c_2), f_D(d_1, d_2)\}$. Figure 1 shows a simple decision tree to decide if a tuple belongs to either



Figure 1: An example of decision tree with Terminal set $\mathcal{T} = \{X, Y\}$ and Function set $\mathcal{F} = \{f_A(a_1, a_2, a_3), f_B(b_1, b_2), f_C(c_1, c_2), f_D(d_1, d_2)\}$

the class X or Y. For example, if a tuple has the value of the attribute A equal to a_1 and that of C equal to c_1 , then it is classified as X. Note that the nodes are labelled directly with the name of the attributes instead of the name of the associated function, for simplicity reasons. To evaluate the accuracy of the decision tree, the fraction of tuples classified into the correct class is computed. The fitness function [21] is defined as the number of training examples classified into the correct class. The CGPC algorithm used for data classification is described in figure 2.

CGPC adopts a cellular model of GP [27]. In the cellular model each individual has a spatial location, a small neighborhood and interacts only within its neighborhood. The main difference in a cellular GP, with respect to a *panmictic* algorithm, is its decentralized selection mechanism and the genetic operators (crossover, mutation) adopted. Cellular models of GP have been used to solve complex problems more accurately and with a minor number of iterations. Although fundamental theory is still an open research line, they have empirically reported as being useful in maintaining diversity, and promoting slow diffusion of solutions through the grid. Part of their behavior is due to a lower selection pressure compared with that of panmictic GP.

CGPC generates a classifier as follows. At the beginning, for each cell, a random individual is generated (step 3) and its fitness is evaluated (step 4). The fitness is the number of training examples classified in the correct class. Then, at each generation, every tree undergoes one of the genetic operators (reproduction (step 19), crossover (steps 9-13), mutation (steps 15-17)) depending on the probability test. If crossover is applied, the mate of the current individual is

1. Let p_c , p_m be crossover and mutation probability							
2. for each point <i>i</i> in grid do in parallel							
3. generate a random individual h_i							
4. evaluate the fitness of h_i							
5. end parallel for							
6. while not MaxNumberOfGeneration do							
7. for each point i in grid do in parallel							
8. generate a random probability p							
9. if $(p < p_c)$							
10. select the cell j , in the neighborhood of i ,							
such that h_j has the best fitness							
11. produce the offspring by crossing h_i and h_j							
12. evaluate the fitness of the offsprings							
13. replace h_i with the best of the two offsprings							
14. else							
15. if $(p < p_m + p_c)$ then							
16. mutate the individual							
17. evaluate the fitness of the new h_i							
18. else							
19. copy the current individual in the population							
20. end if							
21. end if							
22.end parallel for							
23. end while							

Figure 2: The algorithm CGPC.

selected as the neighbor having the best fitness, and the offspring is generated. The current tree is then replaced by the best of the two offsprings if the fitness of the latter is better than that of the former. After the execution of the number of generations defined by the user, the individual with the best fitness represents the classifier.

3.2 The k-means algorithm for clustering classification trees

The algorithm k-means [13] is a well known clustering method that partitions a set of objects into k groups so that the intracluster similarity is high but the intercluster similarity is low. Cluster similarity is measured with respect to the mean value of the objects in a cluster, which can be considered as the cluster's center. The algorithm first randomly selects k objects, and assigns the remaining objects to the most similar cluster, where similarity is computed as the distance between the object and the center of the cluster. After that, the new mean values of the clusters are computed and this process is repeated until the criterion function converges. Typically, the squared-error criterion is used, defined as $E = \sum_{i=1}^{k} \sum_{p \in C_i} dist(p, m_i)^2$, where E is the sum of square error for all the objects, dist is a distance measure, generally the Euclidean distance, p is an object, and m_i is the mean of cluster C_i . Both p and m_i are multidimensional objects.

In order to apply the *k*-means algorithm to a population of trees, it is necessary to specify the concept of distance between two individuals. To this end, we represent each classification tree *h* by a couple (f, e), where *f* is its fitness value and *e* is its distance from the empty tree Φ , considered as the origin tree. This representation allows to take into account both the the concepts of phenotypic (i.e. based on fitness) and genotypic (i.e. based on the syntactical structure of individuals) diversity of the tree population [8]. The metric adopted to measure the structural distance between two genetic trees is that introduced by Ekárt and Németh [14].

The distance between two trees h_1 and h_2 is calculated in three steps: (1) h_1 and h_2 are overlapped at the root node and the process is applied recursively starting from the leftmost subtrees. (2) For each pair of nodes at matching positions, the difference of their codes (possibly raised to an exponent) is computed. (3) The differences computed in the previous step are combined in a weighted sum.

Formally, the distance of two trees h_1 and h_2 with roots R_1 and R_2 is defined as:

$$dist(h_1, h_2) = d(R_1, R_2) + \frac{1}{H} \sum_{i=1}^{m} dist(child_i(R_1), child_i(R_2))$$

where: $d(R_1, R_2) = (|c(R_1) - c(R_2)|)^z$, c is a coding function $c : \{\mathcal{T} \cup \mathcal{F}\} \to \mathcal{N}$ that assigns a numeric code to each node of the tree, $child_i(Y)$ is the i^{th} of the m possible children of a generic node Y, if $i \leq m$, or the empty tree otherwise. The constant H is used to give different weights to nodes belonging to different levels and z is a constant such that $z \in \mathcal{N}$.

For the example data set of the previous section an encoding could be: c(A)=1, c(B)=2, c(C) = 3, c(D)=4, c(X)=5, c(Y)=6.

Figure 3 shows two trees h_1 (figure 3(a)) and h_2 (figure 3(b)) with the weighted coding of each node, and their overlapping (figure 3(c)). Corresponding nodes are enclosed in the rectangular boxes. The distance between h_1 and h_2 , fixed H = 4 and z = 1, is computed as follows: $dist(h_1, h_2) = (|1 - 1|) + (|\frac{3}{4} - \frac{2}{4}| + |\frac{5}{4} - \frac{5}{4}| + |\frac{4}{4} - \frac{6}{4}|) + (|\frac{5}{16} - \frac{5}{16}| + |\frac{6}{16} - \frac{6}{16}| + |\frac{5}{16} - 0| + |\frac{5}{16} - 0|) = 1.31$

When computing the distance between a tree h and the empty tree Φ , $dist(h, \Phi)$ gives simply a weighted sum of the codes associated with the attributes appearing in the tree.

Once for each tree the couple (f, e) has been computed, since both f and e are numbers, the k-means algorithm employs the Euclidean distance to the tree population by using this two dimensional representation.



Figure 3: Two example trees ((a) and (b)) and the overlapped tree (c) to compute their distance.

3.3 The distributed ClustBoostCGPC algorithm to build GP ensemble

ClustBoostCGPC is a new ensemble learning algorithm for constructing GP ensembles. The idea is to incorporate different GP classifiers, each trained on different parts or aspects of the training set, so that the ensemble can better learn from the whole training data. *ClustBoostCGPC* applies the boosting technique in a distributed hybrid model of parallel GP and uses a clustering-

based selective algorithm to maintain the diversity of the ensemble by choosing in each population the most accurate predictors of each group.

Our approach aims at emphasizing the cooperation among the individuals of the population (classifiers) using a hybrid model of parallel GP. It combines the island and cellular models of GP to enhance accuracy and to reduce performance fluctuation of the programs produced by GP. We used a hybrid model essentially for two reasons. First, the island model represents the best distributed implementation of GP that makes use of the domain decomposition technique. Second, the cellular model in each island allows the generation of classifiers with better accuracy and reduced tree size.

The island model is based on subpopulations created by dividing the original population into disjunctive subsets of individuals, usually of the same size. Each subpopulation is assigned to an island and a standard (panmictic) GP algorithm is executed on it. Occasionally, migration process between subpopulations is carried out after a fixed number of generations. The hybrid model modifies the island model by substituting the standard GP algorithm with a cellular GP algorithm [16]. The introduction of the cellular approach improves the exploration capabilities of the algorithm because of a lower selection pressure that promotes a slow diffusion of solutions through the grid. In our model we use the CGPC algorithm in each island. Each island operates in parallel on a subset of the tuples of the training set. The training and combination of the individual classifiers are carried together in the same learning process by a cooperative approach. Our model is based on the coevolution of different subpopulations of classifiers and a migration process that transfers asynchronously individuals among subpopulations.

In order to improve the prediction accuracy achieved by an ensemble, we need to ensure accuracy of classifiers and diversity among them. Although GP does not require any change in a training data to generate individuals of different behaviors, in [17] it is showed that GP enhanced with a boosting technique improves both the prediction accuracy and the running time with respect to the standard GP. *ClustBoostCGPC* combines the boosting method and the distributed hybrid model of GP to iteratively build an ensemble of classification trees through a fixed number of rounds. The selection, at each round, of classifiers satisfying both high diversity and accuracy requirements, is a difficult optimization task. To this end in *ClustBoostCGPC* we applied a method that gradually achieves diversity and accuracy. First, we employ the k-means clustering algorithm to divide all individuals of each subpopulation into groups (clusters) according to similarity of the classifiers. Then, the most accurate individual in each group, i.e. that having the best fitness value, is selected.

A more formal description of the algorithm, in pseudo-code, is shown in figure 4. Let a network of P nodes be given, each having a training set S_j of size n_j . At the beginning, for every node N_j , j = 1, ..., P, a subpopulation Q_j is initialized with random individuals and the weights of the training instances are set to $1/n_j$ (steps 1-4). Each subpopulation Q_j is evolved for a fixed number of generations (step 7) and trained on its local training set S_i by running a copy of the CGPC algorithm (figure 2). After that, the evolved population of trees is clustered by using the k-means algorithm [13] and k groups of individuals are determined (step 8). For each group, the tree having the best fitness is chosen as representative of the cluster and output as the hypothesis computed. Then the k individuals of each subpopulation are exchanged among the P nodes (step 9) and constitute the ensemble of predictors used to determine the weights of the examples for the next round. The error ϵ^t is computed by summing the weights of the misclassified tuples (steps 10-12). The weights for the next trial (step 15) are obtained by multiplying the weight of the correctly classified examples by avg_beta , that is the mean of the $\beta^t = \epsilon^t/(1-\epsilon^t)$ values (steps 13-14) of the k weak hypotheses. Since avg_beta is less than 1, "easy" examples (i.e. already correctly classified) get a lower weight, while "hard" examples, that tend to be misclassified, get higher weights. The boosted classifier gives the class label ythat maximizes the sum of the weights of the weak hypotheses predicting that label, where the weight is defined as $ln(1/\beta^t)$ (step 20). Note that higher the weight of a weak hypothesis, lower the misclassification error rate of the corresponding classifier.

We implemented ClustBoostCGPC using a distributed infrastructure and a distributed framework to run GP. The software architecture of ClustBoostCGPC is illustrated in figure 5.

We used dCAGE (distributed Cellular Genetic Programming System) a distributed envi-

Given a network constituted by P nodes, each having a data set S_i of size n_i 1. For j = 1, 2, ..., P (for each island in parallel) **Initialize** the weights $w_i^1 = \frac{1}{n_i}$ for $i = 1, \ldots, n_j$, 2.where n_j is the number of training examples on each node j. 3. **Initialize** the subpopulation Q_j , for j = 1, ..., P with random individuals 4. end parallel for 5. For $t = 1, 2, 3, \ldots, T$ For j = 1, 2, ..., P (for each island in parallel) 6. 7. **Train** CGPC on the partition S_i using a weighted fitness according to the distribution w^t 8. Run the k-means algorithm to compute k weak hypotheses $h_{j_1,t}...h_{j_k,t}: \mathcal{X} \to \mathcal{Y}$ **Exchange** the hypotheses $h_{j_c,t}$ $c = 1, \ldots, k$ among the P nodes 9. if arg max $h_{j_c,t}(x_i) \neq y_i$ $D_{j_c} = 1$ else $D_{j_c} = 0$ Compute the error $\epsilon_{j_c}^t = \sum_{i=1}^n w_i^t D_{i_c}$ Set $\beta_{j_c}^t = \epsilon_{j_c}^t / (1 - \epsilon_{j_c}^t),$ 10. 11. 12.13.**Compute** $avg_beta_j^t = \frac{\sum_{c=1}^k \beta_{j_c}^t}{k}$ **Update** the weights $w_i^{t+1} = avg_beta_j^t \times w_i^t$ if $h_{j,t}(x_i) = y_i$ 14. 15.end parallel for 16.17. end for t18. output the hypothesis : $h_f = \arg \max \left(\sum_{t=1}^T \sum_{j=1}^P \sum_{c=1}^k \log(\frac{1}{\beta_{j_c}^t}) D_{j_c}^t \right)$ where $D_{j_c}^t = 1$ if $h_{j_c,t}(x_i) = y_i, 0$ otherwise 20.21.

Figure 4: The algorithm CLUSTBOOSTCGPC



Figure 5: Software architecture of ClustBoostCGPC.

ronment to run genetic programs by an island model, which is an extension of [16]. dCage has been modified to support the hybrid variation of the classic island model.

In the new implementation, to take advantage of the cellular model of GP, the islands are evolved independently using the CGPC algorithm, and the outermost individuals are asynchronously exchanged. The training sets S_i , i = 1, ..., P assigned to each of the P islands can be thought as portions of the overall data set. The size of each subpopulation $Q_i, i = 1, ..., P$ present on a node, must be greater than a threshold determined from the granularity supported by the processor. Each node, using a training set S_i and a subpopulation Q_i , implements a classifier process $CGPC_i$ as learning algorithm and generates a population of classifiers. dCAGEdistributes the evolutionary processes (islands) that implement the classification models over the network nodes using a configuration file that contains the configuration of the distributed system. dCAGE implements the hybrid model as a collection of cooperative autonomous islands running on the various hosts within an heterogeneous network that works as a peer-to-peer system. The MPI (Message Passed Interface) library is used to allow cooperation among the islands. Each island, employed as a peer, is identical to each other. At each round, a *collector* process collects the GP classifiers from the other nodes, handling the fusion of the results on behalf of the other peers, and redistributes the GP ensemble for future predictions to all the network nodes.

The configuration of the structure of the processors is based on a ring topology and a classifier process is assigned to each. During the boosting rounds, each classifier process maintains the local vector of the weights that directly reflect the prediction accuracy on that site. At every boosting round the hypotheses generated by each of these classifiers ($CGPC_i$ in Figure 5) are clustered by employing the standard k-means algorithm. Then, the most accurate classifier in each group is selected to be included in the ensemble of predictors.

Next, the ensemble built so far is broadcasted to each classifier process to locally recalculate the new vector of the weights and a copy of the ensemble is stored in a repository. After the execution of the fixed number T of boosting rounds, the classifiers stored in the repository are used to evaluate the accuracy of the classification algorithm.

It is worth to point out that, though ClustBoostCGPC and BoostCGPC build an ensemble of classifiers for the task of data classification, there are some main differences between the two approaches.

ClustBoostCGPC is a distributed algorithm that runs the boosting technique on a hybrid model of parallel GP by combining the island and cellular models. Thus it assumes that each node has its own population and its own data set and that the classification algorithm CGPCbe trained on the local data there contained.

On the other hand, BoostCGPC implements the boosting technique on a parallel computer by adopting the parallel cellular model of GP. In this case, if the number of processors at disposal to run the algorithm is P, the population is partitioned in P subpopulations, one for each processor, and P subsets of tuples are created by uniformly sampling instances from the overall training set with replacement.

Another main difference regards the individuals selected for participating to the ensemble.

After a number of generations, *BoostCGPC* chooses the predictor with the best fitness. *ClustBoostCGPC*, instead, applies the clustering algorithm to the population of trees and picks the individual of each cluster having the best fitness. Though this policy reveals to be beneficial for the accuracy of the method, as experimental results show, it introduces a memory overhead. The next section suggests the use of pruning strategies that partially overcome this problem.

4 Reducing the size of the ensemble

A drawback of the method proposed, and of the ensemble methods in general, is the large amount of memory required to maintain the classifiers. In our case, the size of the ensemble increases as the number of clusters and the number of nodes of the network increase. Thus we could ask if it it possible to discard some of the predictors generated and still obtain comparable accuracy. This approach is well known in the literature and it is called *pruning* [24] or *thinning* [3] the ensemble. Pruning the ensemble requires a strategy to choose the classifiers to remove. There is a general agreement that the predictors forming the ensemble have to be both diverse and accurate. A pruning policy thus identifies the most similar classifiers and removes them. The concept of similarity in this context plays a central role. In the Machine Learning community diversity means that the predictors have to make independent classification errors, i.e. they disagree with each other. A disagreement measure used in [24] is, for example, the κ statistics [1]. In the Genetic Programming community the concept of diversity is perceived in a different way [7, 9]. In particular it reflects the structural diversity of the genetic programs in a generation [14]. In this paper we adopt different diversity measures to choose the trees to prune. In the experimental results we compare them and we show that the ensemble can be quite substantially pruned without increasing misclassification errors; indeed, up to 30% of pruning, ensemble accuracy increases.

The first two diversity measures used are the pairwise distance between two trees (denoted *pairwise*), and the distance of a tree from the empty tree (denoted *origin*), introduced in subsection 3.2.

The third measure is the κ statistics, defined as follows. Given two classifiers h_i and h_j , where $h_i, h_j : \mathcal{X} \to \mathcal{Y}$, consider the following $|\mathcal{Y}| \times |\mathcal{Y}|$ contingency table M. For elements $a, b \in \mathcal{Y}$, define $M_{a,b}$ to contain the number of examples x in the training set for which $h_i(x) = a$ and $h_j(x) = b$.

If h_i and h_j give identical classifications, all non-zero counts will appear along the diagonal. If h_i and h_j are very different, then there should be a large number of counts off the diagonal.

Let

$$\Theta_1 = \frac{\sum_{a=1}^{|\mathcal{Y}|} M_{a,a}}{N}$$

be the probability that two classifiers agree, where N is the size of the training set and $|\mathcal{Y}|$ is the number of different classes. Let also

$$\Theta_2 = \sum_{a=1}^{|\mathcal{Y}|} \left(\frac{\sum_{b=1}^{|\mathcal{Y}|} M_{a,b}}{N} \frac{\sum_{b=1}^{|\mathcal{Y}|} M_{b,a}}{N}\right)$$

be the probability that two classifiers agree by chance, given the observed counts in the table. Then the κ measure of disagreement between classifiers h_i and h_j is defined as

$$\kappa(h_i, h_j) = \frac{\Theta_1 - \Theta_2}{1 - \Theta_2}$$

Dataset	Attr.	Tuples	Classes
Adult	14	48842	2
Census	41	299285	2
Covtype	54	581012	7
Mammography	10	11183	2
Phoneme	5	5404	2
Satimage	$\overline{36}$	6435	6
Segment	19	2310	7

Table 1: Data sets used in the experiments

A value of $\kappa = 0$ implies that $\Theta_1 = \Theta_2$ and the two classifiers are considered different. A value of $\kappa = 1$ implies that $\Theta_1 = 1$, which means that the two classifiers agree on each example.

Thus a pruning strategy first computes the κ , origin, and pairwise measures and then chooses the predictors to eliminate in the following way.

If the *origin* measure is used, the predictors h_i are ordered in increasing order of $dist(h_i, \Phi)$ and eliminated by starting with that having the highest value until the pruning percentage fixed has been reached.

If the *pairwise* (κ) measure is adopted, the distance $dist(h_i, h_j)$ ($\kappa(h_i, h_j)$) values are ordered in increasing order. The pruning strategy eliminates the pairs (h_i, h_j) of classifiers having the lowest value of $dist(h_i, h_j)$ (the highest value of $\kappa(h_i, h_j)$), i. e. the more similar, considering them in increasing order of dist (decreasing order of κ) until the pruning percentage fixed has been reached.

5 Experimental Results

In this section ClustBoostCGPC and BoostCGPC are compared on 7 data sets. Two data sets (*Census* and *Covtype*) are from the UCI KDD Archive¹, three (*Segment*, *Satimage*, and Adult) are taken from the UCI Machine Learning Repository ², one (*Phoneme*) is from the ELENA project ³, and one (*Mammography*) is a research data set used in [11]. The size and

¹http://kdd.ics.uci.edu/

 $^{^{2}}$ http://www.ics.uci.edu/~mlearn/MLRepository.html

 $^{^3 {\}rm ftp.dice.ucl.ac.be}$ in the directory pub/neural/ELENA/databases

Name	Value
max_depth_for_new_trees	6
max_depth_after_crossover	17
max_mutant_depth	2
grow_method	RAMPED
selection_method	GROW
crossover_func_pt_fraction	0.7
crossover_any_pt_fraction	0.1
fitness_prop_repro_fraction	0.1
parsimony_factor	0

Table 2: Main parameters used in the experiments

Table 3: Comparison of the misclassification error rate of BoostCGPC and ClustBoostCGPC with different ensemble sizes.

Dataset	BoostCGPC	BoostCGPC	BoostCGPC	ClustBoostCGPC	ClustBoostCGPC
	100 classifiers	500 classifiers	1000 classifiers	500 classifiers	1000 classifiers
Adult	17.231 ± 0.164	16.29 ± 0.157	15.85 ± 0.164	14.749 ± 0.163	14.641 ± 0.161
Census	6.12 ± 0.045	5.76 ± 0.045	5.51 ± 0.046	4.695 ± 0.042	4.681 ± 0.041
Covtype	33.374 ± 0.468	32.64 ± 0.463	32.81 ± 0.455	30.85 ± 0.453	30.044 ± 0.442
Mammography	2.159 ± 0.099	1.89 ± 0.097	1.92 ± 0.097	1.309 ± 0.093	1.304 ± 0.091
Phoneme	19.121 ± 0.475	18.03 ± 0.460	18.38 ± 0.474	16.968 ± 0.462	16.918 ± 0.448
Satimage	21.398 ± 0.573	20.68 ± 0.566	20.83 ± 0.574	20.22 ± 0.552	20.185 ± 0.543
Segment	13.452 ± 0.421	13.01 ± 0.406	13.22 ± 0.428	12.127 ± 0.418	12.114 ± 0.417

class distribution of these data sets are described in table 1.

The experiments were performed using a network composed by 10 1.133 Ghz Pentium III nodes having 2 Gbytes of Memory, interconnected over high-speed LAN connections.

All results were obtained by averaging over 50 runs by using 70% of the data sets for training and the remaining 30% for testing. In order to do a fair comparison between ClustBoostCGPC, and BoostCGPC we used a network of 10 nodes for both algorithms. The number T of rounds was 10, population size 100 on each node, number of generations 100 (for a total number of generations $100 \times 10=1000$), and number of clusters fixed for ClustBoostGPC 5 and 10. Thus BoostCGPC generated 100 classifiers, while ClustBoostCGPC, in one run 500 predictors, and in the other run 1000 predictors. However, the size of the ensembles for ClustBoostCGPCis greater than that of BoostCGPC. To analyze how the former algorithm performs when the

Dataset	ClustBoostCGPC	C4.5	BoostC4.5	SVM	BoostSVM
Adult	14.749	15.3	15.1	16.4	16.8
Census	4.695	4.9	4.8	6.2	6.1
Covtype	30.850	17.2	17	-	-
Mammography	1.309	1.7	1.8	1.8	1.8
Phoneme	16.968	20.9	20.4	17.7	17.5
Satimage	20.220	15.6	15.2	15.6	14.3
Segment	12.127	11.5	10.7	8.57	7.2

Table 4: Comparison of the misclassification error rate of ClustBoostCGPC and C4.5, SVM, and their boosted versions.

number of predictors in the ensemble is equal to that in the latter, when executing BoostCGPC, we considered the first 5 and 10 fittest individuals from each subpopulation, at each round. In this way we obtained other two ensembles of size 500 and 1000.

A main difference between ClustBoostCGPC and BoostCGPC regards the partitioning of the training sets on the nodes of the network. ClustBoostCGPC runs on a distributed environment where it is supposed that each node has its own data set. In order to simulate this kind of situation, each data set has been equally partitioned among the 10 nodes. Thus each node contains 1/10 of the training set. BoostCGPC runs on a parallel computer, thus according to the sequential AdaBoost approach, it creates 10 subsets of tuples of size 1/10 the overall training set by uniformly sampling instances with replacement. The parameters used for the experiments are shown in table 2.

The main objectives of the experiments have been to investigate the influence of the clustering approach on the accuracy when different number of clusters are chosen, and to analyze and compare the pruning strategies described in the previous section.

Regarding the first objective, ClustBoostCGPC has been executed by fixing the number of clusters to 5 and 10, thus by using an ensemble of 500 an 1000 predictors, and compared with BoostCGPC, that uses an ensemble of 100, 500, and 1000 predictors, obtained as explained above. Table 3 shows the classification errors of the two algorithms. The table shows that for all the data sets the clustering strategy sensibly improves the accuracy of the method. For example, on the Adult data set ClustBoostCGPC (5 clusters) obtains an error of 14.749 instead of 17.231,

16.29, 15.85 of *BoostCGPC* with ensemble size 100, 500, and 1000 respectively. The table points out that the clustering approach is meaningful because the choice of the best individuals in the clustered populations produces a much better result with respect to choosing either the best, or the best five, or the best ten classification trees. However, as the table shows, augmenting the number of clusters is no more beneficial because the reduction of the misclassification error rate is minimal.

Table 4 compares ClustBoostCGPC (ensemble size 500) with the other well known classifications methods C4.5, SVM and their boosted versions. We used the implementations contained in the WEKA [31] open source software available at http://www.cs.waikato.ac.nz/ml/weka/. The table shows that ClustBoostCGPC outperforms the other approaches on four out of the seven data sets. Regarding Covtype, the algorithms SVM and boosted SVM implemented in WEKA were not able to give an answer because of the size of the data set.

Using an ensemble of 500 predictors instead of 100 needs a larger amount of memory to store all the classifiers. Thus the improved accuracy is obtained at the cost of higher storage requirements. In the second set of experiments we show that the ensemble can be substantially pruned without decreasing performance. To this end we considered the ensemble of 500 predictors and we applied the pruning strategies described in the previous section.

Table 5 reports the results of the different pruning strategies for all the data sets. The percentages of pruning experimented are 10%, 20%, 50%, and 80% of the ensemble. The table reports in the column named Err the misclassification error rate of the ensemble pruned of the percentage showed in the corresponding row. In column GainC the relative gain in percentage of the pruned ensemble with respect to the complete ensemble generated by ClustBoostCGPC. In column GainB the relative gain in percentage of the pruned ensemble by BoostCGPC. A positive value means that the misclassification error rate is diminished, while a negative one that it has increased. To statistically validate the results, we performed a two-tailed paired t-test at 95% confidence interval. The values in bold of the columns Err highlight the percentage of training set needed by ClustBoostCGPC to obtain a lower error, meaningful with respect to the statistical test.

		origin			pairwise			kappa		
		Err	GainC	GainB	Err	GainC	GainB	Err	GainC	GainB
	10%	14.711	0.26%	14.62%	14.462	1.95%	16.07%	14.734	0.10%	14.49%
Adult	20%	14.971	-1.51%	13.12%	14.742	0.05%	14.44%	15.042	-1.99%	12.70%
	50%	15.425	-4.58%	10.48%	16.032	-8.70%	6.96%	15.823	-7.28%	8.17%
	80%	19.281	-30.73%	-11.90%	22.469	-52.34%	-30.40%	23.856	-61.74%	-38.45%
	10%	4.582	2.40%	25.13%	4.289	8.64%	29.92%	4.453	5.15%	27.24%
Census	20%	4.744	-1.04%	22.49%	4.706	-0.24%	23.10%	4.768	-1.56%	22.09%
	50%	5.073	-8.06%	17.11%	4.944	-5.31%	19.22%	5.085	-8.32%	16.91%
	80%	7.901	-68.30%	-29.10%	7.542	-60.65%	-23.24%	7.988	-70.15%	-30.52%
	10%	30.679	0.55%	8.08%	30.128	2.34%	9.73%	30.203	2.10%	9.50%
Covtype	20%	30.904	-0.18%	7.40%	30.355	1.60%	9.05%	30.800	0.16%	7.71%
	50%	32.322	-4.77%	3.15%	30.952	-0.33%	7.26%	31.012	-0.53%	7.08%
	80%	34.188	-10.82%	-2.44%	33.681	-9.18%	-0.92%	33.955	-10.06%	-1.74%
	10%	1.297	0.95%	39.93%	1.223	6.60%	43.35%	1.265	3.39%	41.41%
Mamm.	20%	1.385	-5.77%	35.85%	1.307	0.18%	39.46%	1.407	-7.45%	34.83%
	50%	1.467	-12.04%	32.05%	1.421	-8.52%	34.18%	1.604	-22.50%	25.71%
	80%	2.302	-75.81%	-6.62%	2.208	-68.63%	-2.27%	2.420	-84.82%	-12.09%
	10%	16.893	0.44%	11.65%	16.528	2.59%	13.56%	16.349	3.65%	14.50%
Phoneme	20%	17.185	-1.28%	10.13%	16.892	0.45%	11.66%	17.002	-0.20%	11.08%
	50%	18.042	-6.33%	5.64%	18.312	-7.92%	4.23%	18.207	-7.30%	4.78%
	80%	19.207	-13.20%	-0.45%	20.209	-19.10%	-5.69%	19.389	-14.27%	-1.40%
	10%	20.184	0.18%	5.67%	20.003	1.07%	6.52%	20.010	1.04%	6.49%
Satimage	20%	20.240	-0.10%	5.41%	20.081	0.69%	6.15%	20.120	0.49%	5.97%
	50%	20.512	-1.44%	4.14%	20.958	-3.65%	2.06%	20.601	-1.88%	3.72%
	80%	22.845	-12.98%	-6.76%	22.696	-12.25%	-6.07%	22.904	-13.27%	-7.04%
	10%	12.027	0.82%	10.59%	11.906	1.82%	11.49%	12.004	1.01%	10.76%
Segment	20%	12.209	-0.68%	9.24%	12.140	-0.11%	9.75%	12.233	-0.87%	9.06%
	50%	12.638	-4.21%	6.05%	12.643	-4.25%	6.01%	12.901	-6.38%	4.10%
	80%	16.467	-35.79%	-22.41%	15.842	-30.63%	-17.77%	15.068	-24.25%	-12.01%

Table 5: Error and gain of pruned ClustBoostCGPC with respect to unpruned ClustBoostCGPC and unpruned BoostCGPC.



Figure 6: Mean performance of pruned ClustBoostCGPC relative to unpruned ClustBoostCGPC with different pruning percentages.

The table clearly shows that up to 50% of pruning, for all the data sets, independently the pruning strategy used, the ensemble can be reduced and still have an error lower than BoostCGPC (see column GainB). For example, the error obtained with the ensemble generated by ClustBoostCGPC on the Census data set pruned of 50% with the *pairwise* measure is 4.944, while that generated by BoostCGPC is 6.12, thus using the former approach gives a gain of 19.22%. It is worth noting that BoostCGPC with ensemble size 500 and 1000 obtains an error of 5.76 and 5.51, respectively, which is higher than the pruned ensemble of 250 predictors. Furthermore, pruning improves the performance of ClustBoostCGPC if 10% of the classifiers are eliminated. Indeed the *pairwise* strategy, for almost all the data sets, allows the pruning up to 20% of predictors and still decrease the misclassification error rate of ClustBoostCGPC. The structural diversity used in GP thus gives better results than the behavioral diversity employed in the Machine Learning community. This result could be explained by the observation that structural diversity means that the classification trees have nodes labelled with different attributes. As a consequence, the pruned ensemble is able to better generalize because of the presence of independent predictors.

Finally, figures 6 and 7 shows the overall performances, averaged for all the data sets, in terms of the relative gain. In particular, figure 6 displays the relative performance of each



Figure 7: Mean performance of pruned ClustBoostCGPC relative to unpruned BoostCGPC with different pruning percentages.

pruning strategy computed as the difference between the corresponding misclassification error rate and that obtained by *BoostCGPC* divided by the gain, that is the difference in percentage points between these errors. A value of 0 means that the pruned ensemble obtains the same performance as *BoostCGPC*, while a value greater than 0 that the pruned ensemble performs better than *BoostCGPC*. Figure 7 shows the same performance results compared with respect to *ClustBoostCGPC*. These two figures summarizes the results of table 5 and clearly point out that the pairwise strategy behaves better than the two others.

As already observed, table 5 points out that, independently the pruning strategy, the deletion of 10% of trees enhance the accuracy of the method, while 20% of pruning is beneficial only for *pairwise* and, as regards *kappa*, for some data sets. Thus we wanted to verify whether the combination of the three strategies could produce better results than a single one. To this end we deleted 20% of trees by choosing 10% of trees with one strategy and 10% with another, i.e. we combined *pairwise* and *kappa*, *pairwise* and *origin*, and *kappa* and *origin*. Then we deleted 30% of predictors by picking 10% of trees with respect to each pruning strategy. Table 6 shows the result of this experiment. In the table p stands for *pairwise*, k for *kappa*, and o for *origin*. The results are very interesting. The deletion of 20% of trees from the ensemble by picking 10% with a strategy and another 10% with another strategy generates an error lower than both the

%. Prun.	Strategy	Adult	Census	Covtype	Mamm.	Phoneme	Satimage	Segment
	No Prun.	14.749	4.695	30.850	1.309	16.968	20.220	12.127
	pairwise	14.742	4.706	30.355	1.307	16.892	20.081	12.140
	kappa	15.042	4.768	30.800	1.407	17.002	20.120	12.333
20%	origin	14.971	4.744	30.904	1.385	17.185	20.240	12.209
	p + k	14.777	4.421	30.224	1.275	16.265	20.116	12.115
	p + o	14.726	4.588	30.205	1.287	16.564	20.049	12.122
	k + o	14.911	4.602	30.414	1.295	16.686	20.101	12.205
	pairwise	15.382	4.807	30.901	1.395	17.581	20.501	12.397
30%	kappa	15.264	4.946	30.871	1.459	17.481	20.322	12.508
	origin	15.152	4.885	31.12	1.407	17.433	20.389	12.359
	p + o + k	15.001	4.863	30.797	1.319	16.393	20.170	12.271

Table 6: Error of ClustBoostCGPC with respect to different pruning strategies.

ensemble pruned of 20% by applying one strategy and the unpruned ensemble. In particular the error of the unpruned ensemble for the *Census*, *Mammography*, and *Phoneme* data sets diminishes from 4.695, 1.309, 16.968 to 4.421, 1.275, 16.265 respectively when the *pairwise* and *kappa* strategies are combined. For *Adult*, *Covtype*, *Satimage*, and *Segment* the reduction from 14.749, 30.850, 20.220, 12.127 to 14.726, 30.205, 20.049, 12.122 respectively is obtained by mixing the *pairwise* and *origin* strategies. An error decrease of the pruned ensemble with respect to the unpruned one is attained also when 30% of classifiers are deleted by putting together the three strategies for the *Covtype*, *Phoneme*, and *Satimage* data sets. In any case, the elimination of 30% of predictors by mixing the *kappa*, *pairwise*, and *origin* strategies is always better than using one of them at a time. These experiments indicate that the ensemble techniques can achieve improved accuracy when good pruning policies are adopted.

6 Discussion

A boosting algorithm based on cellular genetic programming to build an ensemble of classifiers has been presented. The approach proposed presents two main novelties. The first is the application of a clustering algorithm to the subpopulations of the network nodes to build the ensemble. The second is the utilization of pruning strategies to discard some of the predictors but maintaining comparable accuracy. Both the ideas revealed successful since the former allows the selection of the most diverse and fittest classification trees. The latter reduces the size of the ensemble, improving the classification accuracy. Experiments on several data sets showed that the choice of the fittest individual in the clustered populations produces a much better result with respect to choosing either the fittest or more than one fittest classification trees. ClustBoostCGPC has been compared with the state of the art classification algorithms C4.5 and SVM. Results showed that ClustBoostCGPC outperforms the other approaches on 4 out of the 7 data sets used. It is worth to point out that the lower accuracy of ClustBoostCGPCwith respect to the other two methods on the three multi-class data sets is due to the fact that ClustBoostCGPC implements the version AdaBoost.M1 of the AdaBoost algorithm. As noted by Freund and Schapire [29], and experimented in [18], when the number of classes is more than two, and this is the case of Covtype, Satimage, and Segment data sets, AdaBoostneeds a more sophisticated error measure that allows the weak learner focusing not only on the hard-to-classify examples, but also on the incorrect labels which are the hardest to discriminate. This error measure is implemented in the AdaBoost.M2 version.

Taking more predictors from each subpopulation contained on the nodes of the network could give rise to criticisms because of the greater storage requirements necessary to maintain the ensemble. We showed that by employing suitable pruning strategies it is possible to select a subset of the classifiers without augmenting misclassification errors; indeed, up to 30% of pruning, ensemble accuracy increases.

7 Conclusions

A distributed Boosting Cellular Genetic Programming Classifier has been presented. The method evolves a population of trees for a fixed number of rounds and, after each round, it chooses the predictors to include into the ensemble by applying a clustering algorithm to the population of classifiers. Pruning strategies to the reduce ensemble size have also been experimented. The method runs on a distributed environment based on a hybrid model that combines the island and cellular models of parallel genetic programming. The combination of these two models provides an effective implementation of distributed GP, and the generation of classifiers with better accuracy and reduced tree size. A main advantage of the distributed architecture is that it enables for flexibility, extensibility, and efficiency since each node of the network works with its local data, and communicate with the other nodes, to obtain the results, only the local model computed, but not the data. Furthermore, this architecture is particularly apt to deal with the enormous amount of data that arrives in the form of continuous streams, generated in many application domains, such as credit card transactional flows, telephone records, sensor network data, network event logs. Future work aims at extending the ensemble approach to process these new kinds of data.

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